



K21U 4550

Reg. No. : .....

Name : .....



V Semester B.Sc. Degree CBCSS (OBE) Regular Examination, November 2021  
(2019 Admn. Only)

**CORE COURSE IN MATHEMATICS**

**5B05 MAT : Set Theory, Theory of Equations and Complex Numbers**

Time : 3 Hours

Max. Marks : 48

**PART – A**

Answer **any four** questions from this Part. **Each** question carries **1** mark.

1. State the Uniqueness theorem.
2. Sum of the roots of the equation  $x^3 - x - 1 = 0$  is \_\_\_\_\_.
3. If  $1 + i$  is a root of a quadratic equation, then the other root will be \_\_\_\_\_.
4. What is a reciprocal equation ?
5. If the discriminant  $\Delta$  of a cubic equation is negative, then it has \_\_\_\_\_.

**PART – B**

Answer **any eight** questions from this Part. **Each** question carries **2** marks.

6. If  $S$  is a finite set and  $T \subseteq S$ , then prove that  $T$  is finite.
7. Transform  $x^3 - 6x^2 + 5x + 12 = 0$  into an equation which lacks the second term.
8. If  $\alpha, \beta, \gamma$  are the roots of the equation  $2x^3 + 3x^2 - x - 1 = 0$ , then find the equation whose roots are  $\alpha - 1, \beta - 1, \gamma - 1$ .
9. State De Gua's rule.
10. Find an upper limit of the positive roots of the equation  $x^3 - 10x^2 - 11x - 100 = 0$ .
11. Write necessary and sufficient condition that the equation  $ax^3 + 3bx^2 + 3cx + d = 0$  has two equal roots.
12. Discuss the character of the roots of the equation  $x^3 + 29x - 97 = 0$  without finding them.
13. Explain the first and second kind reciprocal equations.
14. Express the complex number  $2 + 2\sqrt{3}i$  in polar form.
15. Find  $\text{Arg}(-1 - i)$ .
16. State general form of De Moivre's theorem.

P.T.O.



## PART – C

Answer **any four** questions from this Part. **Each** question carries **4** marks.

17. State and prove Cantor's theorem.
18. Use Descartes rule of signs to show that  $x^7 - 3x^4 + 2x^3 - 1 = 0$  has at least four imaginary roots.
19. If  $a + b + c = 0$ , then show that  $a^5 + b^5 + c^5 = 5abc(ab + bc + ca)$ .
20. Solve  $6x^5 + 11x^4 - 33x^3 - 33x^2 + 11x + 6 = 0$ .
21. Solve  $y^3 - 7y^2 + 36 = 0$ , where the difference between two of the roots is five.
22. For any two complex numbers  $a$  and  $b$ , prove that
$$\left| a + \sqrt{a^2 - b^2} \right| + \left| a - \sqrt{a^2 - b^2} \right| = |a + b| + |a - b|.$$
23. If  $z = 1 + i$ , then find  $(1 + i)^{101}$ .

## PART – D

Answer **any two** questions from this Part. **Each** question carries **6** marks.

24. Prove that the set of all rational numbers is denumerable.
  25. Find the rational roots of the equation  $x^3 - 5x^2 - 18x + 72 = 0$ .
  26. Explain the Cardan's solution for general cubic equation.
  27. Find all the fourth roots of unity and locate them graphically.
-