

K23U 1992

Reg. No. :

Name :

II Semester B.Sc. Degree (CBCSS – OBE – Regular/Supplementary/ Improvement) Examination, April 2023 (2019 Admission Onwards) CORE COURSE IN MATHEMATICS 2B02 MAT : Integral Calculus and Logic

Time : 3 Hours

Max. Marks: 48

SECTION - A

Short Answer Questions. Answer any 4.

- 1. Find the value of $\int_{0}^{\pi/2} \cos^7 x \, dx$.
- 2. Find a polar equation for the circle $(x 2)^2 + y^2 = 4$.
- 3. What is Tautology ?
- 4. Write the principle of double negation.
- Write the contrapositive of the implication "If I am in Chicago, then I am in Illinois". (4×1=4)

SECTION - B C

Short Essay Questions. Answer any 8.

- 6. Show that $\sinh 2x = 2 \sinh x \cosh x$.
- 7. Evaluate $\int_{0}^{1} x^{2} (1-x^{2})^{3/2} dx$.
- 8. Evaluate ∫cosec⁵xdx.
- 9. Calculate $\iint_{R} f(x, y) dA$ for $f(x, y) = 100 6x^2y$ and $R : 0 \le x \le 2, -1 \le y \le 1$.
- 10. Graph the sets of points whose polar coordinates satisfy the conditions $1 \le r \le 2$ and $0 \le \theta \le \frac{\pi}{2}$.

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- 11. Write the equations relating spherical coordinates to Cartesian and cylindrical co-ordinates.
- 12. Find the Jacobian for the polar coordinate transformation $x = r \cos \theta$, $y = r \sin \theta$.
- 13. Find the minimum number of intervals required to evaluate $\int_0^1 \ln(1+x) dx$ using Simpson's 1/3 rule with an accuracy of 10^{-6} .
- 14. Evaluate $\int_{0}^{2} \frac{dx}{x^{2} + 2x \pm 10}$ using Simpson's rule with n = 2.
- 15. Find the truth set T_p of the propositional function p(x) given by "x + 5 > 1", defined on the P = {1, 2, 3,...}.
- 16. Negate the statement "All students live in dormitories".

(8×2=16)

SECTION - C

Essay Questions. Answer any 4.

- 17. Evaluate $\int_{0}^{\ln 2} 4e^{x} \sinh x dx$
- 18. Derive the reduction formula for $\int \sin^n x \, dx$
- 19. Find the area enclosed by the lemniscate $r^2 = 4 \cos 2\theta$
- 20. Evaluate $\int_{0}^{1} \int_{0}^{1-x} \sqrt{x+y} (y-2x)^{2} dy dx$.
- 21.-Use truth table to show that $\neg (p \land q) \equiv \neg p \lor \neg q$.
- 22. If m and n are natural numbers such that $m + n \ge 20$ then show that either $m \ge 10$ or $n \ge 10$.
- Give a direct proof to the theorem "The square of an odd integer is also an odd integer". (4×4=16)

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SECTION - D

Long Essay Questions. Answer any 2.

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- 24. Obtain a reduction formula for $\int x^n e^{-x} dx$ and hence show that the improper integral $\int_0^\infty x^n e^{-x} dx = n!$, where n is any positive integer.
- 25. Using polar integration, find the area of the region R in the xy plane enclosed by the circle $x^2 + y^2 = 4$, above the line y = 1, and below the line $y = \sqrt{3}x$.
- 26. Evaluate $\int_0^1 \frac{dx}{3+2x}$ using trapezoidal rule with n = 2. Compare with the exact solution. Also find the number of sub intervals required if the error is to be less than 5×10^{-4} .
- 27. Prove that there are infinitely many prime numbers.

 $(2 \times 6 = 12)$