Reg. No. :

Name :

III Semester B.Sc. Degree (CBCSS - Suparable) Examination, November 2020 (2014 - '18 Admns.) COMPLEMENTARY COURSE IN STATISTICS FOR GEOGRAPHY/ PSYCHOLOGY CORE 3C03STA : Probability and Distribution Theory

Time: 3 Hours

Max, Marks: 40

Instruction : Use of Calculators and Statistical Tables are Permitted.

PART - A

(Short Answer)

Answer all the questions.

1. State addition theorem of probability.

2. Define a random variable and give an example.

3. If variance of X is 3, what is var(2X-3)?

4. What do you mean by standard Normal distribution ?

5. Define Exponential distribution.

6. If X~N (μ , σ^2), what is the distribution of \overline{X} , the sample mean ?

PART - B

(Short Essay)

Answer any six questions.

- 7. Show that $P(A^c) = 1 P(A)$.
- 8. Write the axiomatic definition of probability.
- 9. State the multiplication theorem probability.
- 10. Discuss the properties of a probability density function of a random variable both in discrete and continuous cases.

 $(6 \times 2 = 12)$

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(6×1=6)

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- 11. Is f(x) = x where $x = \frac{1}{16}, \frac{3}{16}, \frac{1}{4}, \frac{1}{2}$ a probability density function ? Why ?
- Find the mean and variance of the Binomial distribution with parameters n = 3 and p=1/3.
- 13. What are the conditions under which binomial distribution tends to Poisson ?

14. Define students t distribution.

PART – C (Essay)

Answer any four questions.

 $(4 \times 3 = 12)$

 $(2 \times 5 = 10)$

15. If A,B and C are any three events, write down the expressions for the events

- i) Only A occurs
- ii) All the three occurs
- iii) None occurs.

16. Find the expectation of X, if x has the probability mass function.

| Х | -1 | -2 | 0 | 1 | 2 |
|--------|------|-----|-----|-----|------|
| P(X=x) | 0.15 | 0.3 | 0.2 | 0.1 | 0.25 |

- Seven coins are tossed simultaneously. Find the probability of getting maximum of 3 heads.
- 18. Show that exponential distribution possesses the lack of memory party.
- 19. List any six properties of Normal distribution.
- 20. State any four applications of Chi-square distribution.

PART - D

(Long Essay)

Answer any two questions.

21. In a bolt factory machines A,B and C manufacture respectively 25%, 35% and 45% of the total of their output 5,4 and 2 percent are defectives. A bolt is drawn at random and found to be defective. What are the probabilities that it was manufactured by machines A,B and C ?

22. If
$$f(x) = \frac{1}{8}$$
 where x = 1, 2, 3, 4, 5, 6, 7, 8

i) Derive the distribution function

- ii) Calculate $P(X \ge 5)$ and
- iii) P(X = even number).
- 23. Four coins are tossed 80 times. The distribution of the number of heads is given below. Fit a Binomial distribution.

| No. of heads | Frequency | |
|--------------|-----------|--|
| 0 | 4 | |
| 1 | 20 | |
| 2 | 32 | |
| 3 | 18 | |
| 4 | 6 | |

- 24. a) Define Chi-square distribution and F distribution.
 - b) Establish the interrelationship between t, F and χ^2 distributions.