

Reg. No. :

Name :

V Semester B.Sc. Degree (C.B.C.S.S. – O.B.E. – Regular/Supplementary/ Improvement) Examination, November 2023 (2019-2021 Admissions) CORE COURSE IN MATHEMATICS 5B05 MAT : Set Theory, Theory of Equations and Complex Numbers

Time : 3 Hours

Max. Marks: 48

PART - A

Answer any 4 questions from this part. Each question carries 1 mark. (4×1=4)

- 1. Give example for a denumerable set.
- If α, β, γ are the root of the equation f(x) = 0, then the equation whose roots are α, β, γ is _____

3. Show that $x^5 - 2x^2 + 7 = 0$ has atleast two imaginary roots.

4. If ω is an imaginary cube root of unity, then the value of $1 + \omega + \omega^2$ is _____

5. What is the value of Arg z for positive real axis, z = x?

PART – B

Answer any 8 questions from this part. Each question carries 2 marks. (8x2=16)

6. Show that the set of all integers is countable.

- 7. If α , β , γ are the root of the equation $ax^3 + bx^2 + cx + d = 0$, then find the values of $\alpha + \beta + \gamma$ and $\alpha\beta\gamma$.
- 8. Find the condition that the cubic equation $x^3 lx^2 + mx n = 0$ should have its roots in arithmetical progression.
- 9. If α , β , γ are the root of the equation $8x^3 4x^2 + 6x 1 = 0$, find the equation whose roots are $2\alpha + 1$, $2\beta + 1$, $2\gamma + 1$.

10. State De Gua's rule.

11. What do you mean by reciprocal equation ? Give an example.

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- 12. Describe the discriminant of the cubic equation $ax^3 + 3bx^2 + 3cx + d = 0$.
- 13. Transform $x^3 6x^2 + 5x + 12 = 0$ into an equation lacking the second term.
- 14. If a, b, c are the roots of the cubic equation $x^3 + px^2 + qx + r = 0$, find the value of $\frac{1}{a^2b^2} + \frac{1}{b^2c^2} + \frac{1}{c^2a^2}$. ollegi
- 15. What are the imaginary cube root of unity ?
- 16. Find the polar form of z = 1 + i.

PART - C

Answer any 4 questions from this part. Each question carries 4 marks. $(4 \times 4 = 16)$

- 17. If A is a set with m elements and B is a set with n elements and if $A \cap B = \phi$, then prove that $A \cup B$ has m + n elements.
- 18. Solve the equation $x^4 2x^3 + 4x^2 + 6x 21 = 0$, given that the sum of the two of its roots is zero.
- 19. Find the rational roots of $x^4 39x^2 + 46x 168 = 0$.
- 20. Solve $6x^5 + 11x^4 33x^2 + 11x + 6 = 0$.
- 21. Describe the behaviour of roots of a cubic equation in terms of its discriminant.
- 22. Find the value of $\sqrt{1+i}$.
- 23. Find the fifth root of (-1)

PART - D

Answer any 2 questions from this part. Each question carries 6 marks.

 $(2 \times 6 = 12)$

- 24. State and prove Cantor's theorem.
- 25. If α , β , γ are the root of the equation $ax^3 + 3bx^2 + 3cx + d = 0$, then find the values of
 - a) $(\alpha^2 + 1) (\beta^2 + 1) (\gamma^2 + 1)$
 - b) $(\beta \gamma)(\gamma \alpha) + (\gamma \alpha)(\alpha \beta) + (\alpha \beta)(\beta \gamma).$
- 26. Find a real root of the $x^3 + x^2 16x + 20 = 0$.
- 27. If z1 and z2 are two complex numbers, prove that
 - a) $|z_1 z_2| = |z_1| |z_2|$
 - b) arg $(z_1 z_2) = \arg z_1 + \arg z_2$.